PMT

(	Question		Marking details	Marks Available	
1	(a)		Reasonable attempt at conservation of momentum (1) e.g. $330\ 000m = \pm 10\ 000m + 6.6 \times 10^{-27} \times v_1$ conservation of momentum applied correctly and values substituted (1) e.g. $330\ 000 \times 3.4 \times 10^{-25} = -10\ 000 \times 3.3 \times 10^{-25} + 6.6 \times 10^{-27} \times v_1$ correct answer = $1.75 \times 10^7$ [m s <sup>-1</sup> ] ( <b>no ecf</b> ) (1)	3	
	(b)	(i)	Any valid answer e.g. impulse ( <b>or</b> force <b>or</b> acceleration <b>or</b> change in momentum) is vertical, gamma has no momentum in horizontal direction, perpendicular directions are independent etc. Accept: no horizontal force	1	
		(ii)	Attempt at using $p = \frac{h}{\lambda}$ (1)	4	
			$E = hf$ and $c = f\lambda$ quoted (or equivalent $E = \frac{hc}{\lambda}$ ) (1)		
			N.B. $p = \frac{E}{c}$ gains 2 marks		
			Correct momentum = $6.33 \times 10^{-22}$ (1) Answer = $\frac{6.33 \times 10^{-22}}{3.3 \times 10^{-25}}$ [1 920 m s <sup>-1</sup> ] (1)		
		(iii)	Method i.e. $\sqrt{10000^2 + 2000^2}$ (1)	4	
			Answer = <b>10 200</b> [m s <sup>-1</sup> ] <b>ecf</b> on $v$ from $(b)(ii)$ (1) Method and correct		
			indication of angle e.g. $\tan^{-1}\left(\frac{2000}{10000}\right)(1)$		
			Answer = $11.5^{\circ}$ or 0.2 [rad] (or 90-11.5 for other angle if indicated etc.) (1)		
			Question 1 Total	[12]	

Q	uestio	on	Marking details	Marks Available	
2	( <i>a</i> )	(i)	(Number of moles) $n = 4.73$ (1)	3	
			Mass = $4 \times 4.73$ or $0.004 \times 4.73$ (or implied) (1)		
			Density = $0.004 \times 4.73 / 0.113 = 0.167 $ (1)		
		(ii)	Either $p = \frac{1}{3}\rho \overline{c^2}$ used or equivalent e.g. $\frac{3}{2}nRT = \frac{1}{2}M\overline{c^2}$ (1)	2	
			1 350 [m s <sup>-1</sup> ] (1)		
	(b)		Density = $0.004 \times 4.73 / 0.212$ or $T = \frac{45000 \times 0.212}{4.73 \times 8.31} \operatorname{ecf}(1)$	3	
			$p = \frac{1}{3}\rho \overline{c^2}$ used or $\frac{3}{2}nRT = \frac{1}{2}M\overline{c^2}$ used or equivalent (1)		
			Answer = $1  230  [m  s^{-1}]  (1)$		
			Question 2 Total	[8]	
3	(a)		Substitution into $v = \sqrt{\frac{GM}{r}}$ (1)	2	
			Answer = $158\ 000\ [m\ s^{-1}]\ (1)$		
	(b)		Measured velocity is greater (1)	3	
			Which implies that the mass is greater (1)		
			Suggests the existence of dark matter (1)		
			Suggests the existence of dark matter (1)		

[5]

Question 3 Total

(	Juestic	on	Marking details	Marks Available	
4	<i>(a)</i>		Mass substituted into $T = 2\pi \sqrt{\frac{m}{k}}(1)$	3	
			$T = \frac{1}{f}$ used or implied (1)		
			Answer = $152 \text{ N m}^{-1} \text{ UNIT mark} (1)$		
	(b)		$3.47 \times 2\pi = 21.803$	1	
	(c)	(i)	$v = \omega A$ [= 1.853] or max PE = max KE (1)	3	
			$KE = \frac{1}{2}mv^2$ used or $= \frac{1}{2}kx^2(1)$		
			Answer = $0.55 [J] (1)$		
		(ii)	Acceleration = $\omega^2 A$ or $F = kA$ Accept $F = kA - mg(1)$	2	
			Answer = $12.9 [N] (1)$		
	( <i>d</i> )		Substitution of values e.g. $-1.4 = 8.5 \sin(21.8 \times 0.1 + \epsilon)$ (1)	3	
			$\sin^{-1}\left(\frac{-1.4}{8.5}\right) = -0.165(1)$		
			$\varepsilon = -2.35$ or equivalent in degree (-135°) or other quadrant (-5.16) ecf on minus sign (1)		
			Question 4 total	[12]	

	Questic	on	Marking details	Marks Available	
5	<i>(a)</i>	(i)	Force per unit mass (this minimalist answer is acceptable unless some contradiction)	1	
		(ii)	Work done per unit mass <u>from infinity</u> (this minimalist answer is acceptable unless some contradiction)	1	
	(b)	(i)	$F = \frac{GMm}{r^2}  \text{used (1)}$	2	
			Answer = $22.8 [N] (1)$		
		(ii)	$PE = [-] \frac{GMm}{r}$ used <b>or</b> equivalent (1)	2	
			Answer = $-13.7 \text{ M}[\text{J}](1)$		
	(c)		$PE = [-] \frac{GMm}{r}$ used or equivalent (1)	2	
			Answer = $-61.8 \text{ M}[\text{ J}]$ (ecf on $-\text{sign}$ ) (1)		
	( <i>d</i> )		Difference in PE attempted (1)	2	
			Correct answer = $48.1 \text{ M}[\text{J}]$ ((b)(ii) – (c)) ecf (1) Answer must be consistent with their signs		
			Question 5 Total	[10]	

	Question	Marking details	Marks Available	
6	(a)	All arrows correct $\checkmark \checkmark$ Directions in line with dotted lines but some (or all) directions inverted $\checkmark$	2	
	(b)	$E = \frac{Q}{4\pi\varepsilon_0 r^2}  \text{used (1)}$ Answer = 1 500 V m <sup>-1</sup> or N C <sup>-1</sup> or equivalent UNIT mark (1)	2	
	(c)	<u>Field of</u> 13 $\mu$ C ×2 <b>and</b> ×12/13 (1) Answer = 222 [V m <sup>-1</sup> ] (1) To the left <b>or</b> implied clearly in the calculation (1)	3	
	(d)	$V = \frac{Q}{4\pi\varepsilon_0 r}  \text{used for 3 charges with } r = 12 \text{ or } 13 (1)$ $V = \frac{1}{4\pi\varepsilon_0} \left( 2\frac{13}{13} - \frac{24}{12} \right) \text{ as shown or equivalent (cm perfectly valid) (1)}$	2	
	(e)	<ul> <li>Any 3 (×1) from:</li> <li>initial total energy is zero / initial and final PE is zero</li> <li>final total energy is zero / initial and final KE is zero</li> <li>initial force is to the right (has to be linked to the field and the negative charge)</li> <li>later the force is to the left (but not a resistive force)</li> </ul>	3	
		Question 6 Total	[12]	

(	Question	Marking details	Marks Available	
7	(a)	$T = 2\pi \sqrt{\frac{(3 \times 10^{10})^3}{6.67 \times 10^{-11} \times (7 \times 10^{29} + 4 \times 10^{28})}}$ (1)	2	
		Answer = $4.65 \times 10^{6}$ [s] (1) (4.78 × 10 <sup>6</sup> s scores 1/2 marks)		
	<i>(b)</i>	$r_1 = \frac{M_1}{M_1 + M_2} d$ used or $M_1 r_1 = M_2 r_2$ used (1)	2	
		Star orbit radius = $0.162 \times 10^{10}$ [m] (1) (0.171 × 10 <sup>10</sup> scores 1/2 marks)		
	(c)	$v = \frac{2\pi r}{T}$ or $v = \omega r$ and $\omega = 2\pi f \operatorname{ecf}$ on $T$ and $r(1)$	4	
		$v = \frac{2\pi \times 0.162 \times 10^{10}}{4.65 \times 10^6} [= 2191] (1)$		
		$\frac{\Delta \lambda}{\lambda} = \frac{v}{c}  \text{attempted or rearranged ecf on } v (1)$		
		Answer = $4.8 \times 10^{-12}$ [m] (1)		
	( <i>d</i> )	Hotter <b>or</b> the Earth is cooler <b>or</b> equivalent (1)	2	
		Due to higher intensity [of e-m radiation] (1) Accept because $5^2 > 20$ or similar		
		Question 7 Total	[10]	

(	Questio	on	Marking details				Marks Available	
8	(a)	(i)	$T=\frac{1}{2}$	2				
			$T = \frac{q}{2}$	28.9×8.31 (=	<b>312.5 K)</b> (1)			
		(ii)	U =	<i>nRT</i> used or	3/2  pV(1)			2
			AB =	-36 400[J] (1	)			
	<i>(b)</i>	(i)	0					1
		(ii)	Valid Acce	2				
			Answ	$ver = -47\ 250$	[J] (1)			
	(c)			AB	BC	CA	ABCA	
			W	0	37.6 kJ	-47.3 k	сJ -9.7 kJ	
			$\Delta U$	-36.4 kJ	33.5 kJ	2.9 k	J O	4
			Q	-36.4 kJ	71.1 kJ	-44.4	kJ -9.7 kJ	
				$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	
				<b>ecf</b> on $\Delta U$	no ecf	<b>ecf</b> on <i>W</i>	<b>ecf</b> on all if $\Delta U \approx 0$ but must make sense	
			Ques	tion 8 Total				[11]